Practice problems for Lecture 2.

1. A Simple Option Pricing Problem in One Period

Riskless bond (interest rate is 50%):

Stock:

$$50$$
 125 50

Derivative security (call option with a strike of 80):

?
$$\checkmark$$

a. What is the portfolio of the stock and the bond that replicates the option?

b. What is the price of the portfolio?

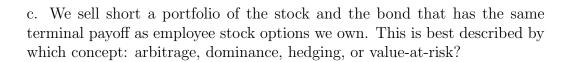
c. What are the risk-neutral probabilities of the two states? Verify that your answer gives the correct price for the stock, the bond, and the option. Reminder: the formula for the risk-neutral probability of an up move is (r-d)/(u-d).

d. (thought question - answer in a sentence or two of ordinary length) Sup-
pose we have inherited many shares of the stock and would like to trade them
to diversify but we are precluded from trading the stock due to terms of an
inheritence. If the inheritence does not preclude trading the option, how can
this help us? (Note: do not perform any computations in this answer.)

2. General Concepts (very short answers)

a. We buy cheap gold futures in one market and sell the identical contract for more in another market to lock in a riskless profit. This is most related to which concept: arbitrage, dominance, hedging, or value-at-risk?

b. If the call option price equals the underlying stock price, we would rather buy the stock than the option because the stock is worth more in most contingencies and is never worth less. This is most related to which concept: arbitrage, dominance, hedging, or value-at-risk?



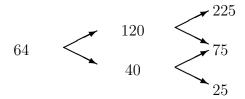
d. Name three types of options on common stock.

3. A Simple Option Pricing Problem in Two Periods

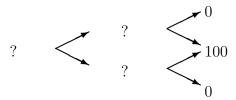
Riskless bond (riskfree interest rate is 25%)

$$16 \longrightarrow 20 \longrightarrow 25$$

Stock price:



Derivative security (European binary/digital option paying 100 when the stock price is between 50 and 100 and paying zero otherwise):



The actual probabilities are 1/3 for up and 2/3 for down at each node.

a. What are the risk-neutral probabilities of up and down? (The risk-neutral probabilities are the same at every node: compute them at the first node. Reminder: the formula for the risk-neutral probability of an up move is (r-d)/(u-d). Advice: check to make sure the stock price is consistent with your answer.)

1	TT71	. 1	1	C . 1	1 .		. 1	1.0
b.	What is	the	value	of the	binary	option	at each	node!

c. In the portfolio strategy that replicates the binary option, what are the holdings in the stock and the bond at the initial node?

d. (thought question – answer in a sentence or two of ordinary length) Suppose you have a view that volatility will be smaller than most people expect. Your investment banker has proposed the purchase of these binary options as a way of profiting if your view is correct. Discuss.